

## XE : ENGINEERING SCIENCES

Duration: Three Hours

Maximum Marks: 100

**Read the following instructions carefully.**

1. Do not open the seal of the Question Booklet until you are asked to do so by the invigilator.
2. Take out the **Optical Response Sheet (ORS)** from this Question Booklet **without breaking the seal** and read the instructions printed on the **ORS** carefully.
3. On the right half of the **ORS**, using **ONLY a black ink ball point pen**, (i) darken the bubble corresponding to your test paper code and the appropriate bubble under each digit of your registration number and (ii) write your registration number, your name and name of the examination centre and put your signature at the specified location.
4. This Question Booklet contains **36** pages including blank pages for rough work. After you are permitted to open the seal, please check all pages and report discrepancies, if any, to the invigilator.
5. There are a total of 65 questions carrying 100 marks. All these questions are of objective type. Each question has only **one** correct answer. Questions must be answered on the left hand side of the **ORS** by darkening the appropriate bubble (marked A, B, C, D) using **ONLY a black ink ball point pen** against the question number. **For each question darken the bubble of the correct answer.** More than one answer bubbled against a question will be treated as an incorrect response.
6. Since bubbles darkened by the black ink ball point pen **cannot** be erased, candidates should darken the bubbles in the **ORS very carefully.**
7. This Question Booklet contains **Eight** sections: **GA** (General Aptitude), **A** (Engineering Mathematics), **B** (Fluid Mechanics), **C** (Materials Science), **D** (Solid Mechanics), **E** (Thermodynamics), **F** (Polymer Science & Engineering) and **G** (Food Technology).
8. Section **GA** (General Aptitude) and Section **A** (Engineering Mathematics) are compulsory. Attempt any **two** optional sections **B** through **G**. Using a **black ink ball point pen**, mark the sections you have chosen by darkening the appropriate bubbles provided on the left hand side of the **ORS**. Also, write the codes of the optional sections in the boxes provided. In case the candidate **does not bubble section codes** corresponding to Optional Section-1 or Optional Section-2 or both, the corresponding sections **will NOT be evaluated.**
9. Questions Q.1 – Q.10 belong to Section **GA** (General Aptitude) and carry a total of 15 marks. Questions Q.1 – Q.5 carry 1 mark each, and questions Q.6 – Q.10 carry 2 marks each.
10. There are 11 questions carrying 15 marks in Section **A** (Engineering Mathematics), which is compulsory. Questions Q.1–Q.7 carry 1 mark each and questions Q.8–Q.11 carry 2 marks each.
11. Each of the other sections (Sections **B** through **G**) contains 22 questions carrying 35 marks. Questions Q.1–Q.9 carry 1 mark each and questions Q.10–Q.22 carry 2 marks each. The 2 marks questions include two pairs of common data questions and one pair of linked answer questions. The answer to the second question of the linked answer questions depends on the answer to the first question of the pair. If the first question in the linked pair is wrongly answered or is unattempted, then the answer to the second question in the pair will not be evaluated.
12. Unattempted questions will result in zero mark and wrong answers will result in **NEGATIVE** marks. For all 1 mark questions,  $\frac{1}{3}$  mark will be deducted for each wrong answer. For all 2 marks questions,  $\frac{2}{3}$  mark will be deducted for each wrong answer. However, in the case of the linked answer question pair, there will be negative marks only for wrong answer to the first question and no negative marks for wrong answer to the second question.
13. Calculator is allowed whereas charts, graph sheets or tables are **NOT** allowed in the examination hall.
14. Before the start of the examination, write your name and registration number in the space provided below using a black ink ball point pen.

<b>Name</b>								
<b>Registration Number</b>	<b>XE</b>							

**General Aptitude (GA) Questions (Compulsory)****Q. 1 – Q. 5 carry one mark each.**

- Q.1 One of the parts (A, B, C, D) in the sentence given below contains an ERROR. Which one of the following is **INCORRECT**?

**I requested that he should be given the driving test today instead of tomorrow.**

- (A) requested that
- (B) should be given
- (C) the driving test
- (D) instead of tomorrow

- Q.2 Which one of the following options is the closest in meaning to the word given below?

**Latitude**

- (A) Eligibility                      (B) Freedom                      (C) Coercion                      (D) Meticulousness

- Q.3 Choose the most appropriate word from the options given below to complete the following sentence:

**Given the seriousness of the situation that he had to face, his \_\_\_ was impressive.**

- (A) beggary                      (B) nomenclature                      (C) jealousy                      (D) nonchalance

- Q.4 Choose the most appropriate alternative from the options given below to complete the following sentence:

**If the tired soldier wanted to lie down, he \_\_\_ the mattress out on the balcony.**

- (A) should take
- (B) shall take
- (C) should have taken
- (D) will have taken

- Q.5 If  $(1.001)^{1259} = 3.52$  and  $(1.001)^{2062} = 7.85$ , then  $(1.001)^{3321} =$

- (A) 2.23                      (B) 4.33                      (C) 11.37                      (D) 27.64

**Q. 6 - Q. 10 carry two marks each.**

- Q.6 A and B are friends. They decide to meet between 1 PM and 2 PM on a given day. There is a condition that whoever arrives first will not wait for the other for more than 15 minutes. The probability that they will meet on that day is

- (A)  $1/4$                       (B)  $1/16$                       (C)  $7/16$                       (D)  $9/16$

- Q.7 The data given in the following table summarizes the monthly budget of an average household.

Category	Amount (Rs.)
Food	4000
Clothing	1200
Rent	2000
Savings	1500
Other expenses	1800

The approximate percentage of the monthly budget **NOT** spent on savings is

- (A) 10%                      (B) 14%                      (C) 81%                      (D) 86%
- Q.8 There are eight bags of rice looking alike, seven of which have equal weight and one is slightly heavier. The weighing balance is of unlimited capacity. Using this balance, the minimum number of weighings required to identify the heavier bag is
- (A) 2                      (B) 3                      (C) 4                      (D) 8
- Q.9 Raju has 14 currency notes in his pocket consisting of only Rs. 20 notes and Rs. 10 notes. The total money value of the notes is Rs. 230. The number of Rs. 10 notes that Raju has is
- (A) 5                      (B) 6                      (C) 9                      (D) 10
- Q.10 **One of the legacies of the Roman legions was discipline. In the legions, military law prevailed and discipline was brutal. Discipline on the battlefield kept units obedient, intact and fighting, even when the odds and conditions were against them.**

Which one of the following statements best sums up the meaning of the above passage?

- (A) Thorough regimentation was the main reason for the efficiency of the Roman legions even in adverse circumstances.
- (B) The legions were treated inhumanly as if the men were animals.
- (C) Discipline was the armies' inheritance from their seniors.
- (D) The harsh discipline to which the legions were subjected to led to the odds and conditions being against them.

## A : ENGINEERING MATHEMATICS (Compulsory)

**Q. 1 – Q. 7 carry one mark each.**

Q.1 For the matrix  $M = \begin{bmatrix} 1 & 4 & 5 \\ 0 & 2 & 6 \\ 0 & 0 & 3 \end{bmatrix}$ , consider the following statements:

P: 3 is an eigenvalue of  $M$ .    Q:  $\begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$  is an eigenvector of  $M$ .    R:  $\begin{bmatrix} 4 \\ 2 \\ 0 \end{bmatrix}$  is an eigenvector of  $M$ .

Which of the above statements are **TRUE**?

- (A) P and Q, but not R                      (B) Q and R, but not P  
(C) P and R, but not Q                      (D) P, Q, and R

Q.2 Taylor series of  $f(x) = \frac{1}{1-x}$  about  $x=0$  is given as  $TS|_f = 1 + x + x^2 + x^3 + \dots$ . This series can be used to evaluate  $f(x)$  for

- (A)  $|x| \neq 1$                       (B)  $x < -1$                       (C)  $|x| < 1$                       (D)  $-1 \leq x < 1$

Q.3 Let  $f(u, v) = u \ln(v)$  and  $F(x, y) = f(u(x, y), v(x, y))$ , where  $u = x/y$  and  $v = x - y$ . Then  $\partial F / \partial y$  is

- (A)  $-\frac{x}{y^2} \ln(x - y) + \frac{x}{y(x - y)}$                       (B)  $-\frac{x}{y^2} \ln v - \frac{u}{v}$   
(C)  $\frac{x}{y^2} \ln v - \frac{u}{v}$                       (D)  $\frac{x}{y^2} \ln v + \frac{x}{yv}$

Q.4 Consider two functions  $f(z) = |z|$  and  $g(z) = \bar{z}$  (conjugate of  $z$ ). Using Cauchy-Riemann conditions, choose the correct answer

- (A) Both  $f$  and  $g$  are analytic                      (B)  $f$  is analytic but  $g$  is not analytic  
(C)  $g$  is analytic but  $f$  is not analytic                      (D) Neither  $f$  nor  $g$  is analytic

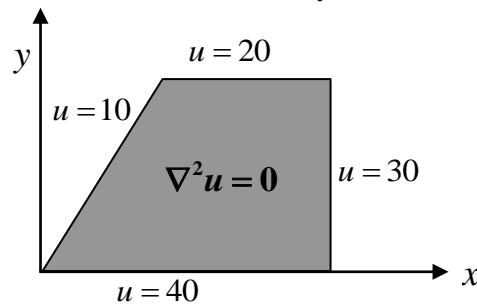
Q.5 For  $f = x^4 - 5xy^2$ , the direction of maximum increase of  $f(x, y)$  at the point (2, 2) is along

- (A)  $3\hat{i} + 10\hat{j}$                       (B)  $-12\hat{i} - 40\hat{j}$                       (C)  $3\hat{i} - 10\hat{j}$                       (D)  $-12\hat{i} + 40\hat{j}$

Q.6 Suppose 50% of the population of a village like oranges, 70% of the population like apples, and 40% like both. If a person is picked at random who likes at least one of these fruits, what is the probability that the person likes oranges?

- (A) 1/8                      (B) 5/12                      (C) 1/2                      (D) 5/8

Q.7 For the solution of  $\nabla^2 u = 0$ , the domain and boundary conditions are shown below.



Which of the following statements is **TRUE**?

- (A) The solution cannot be obtained using separation of variables because the governing equation is non-separable.
- (B) The solution cannot be obtained using separation of variables because all the boundary values are non-zero.
- (C) The solution cannot be obtained using separation of variables because not all the boundaries are along constant coordinate lines.
- (D) The solution can be obtained by separation of variables.

**Q. 8 - Q. 11 carry two marks each.**

Q.8 If  $f(x) = x \sin(x)$  and  $g(x) = |x| \sin(x)$ , then

- (A)  $g(x) = |f(x)|$
- (B)  $g(x)$  is an even function
- (C) The  $x$ -coordinates corresponding to the various local maxima are identical for both  $f(x)$  and  $g(x)$
- (D)  $g(x)$  is differentiable at  $x = 0$

Q.9 The general solution of  $\frac{d^4 y}{dx^4} - 2 \frac{d^3 y}{dx^3} + 2 \frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + y = 0$  is

- (A)  $c_1 e^x + c_2 x e^x + c_3 \cosh(x) + c_4 \sinh(x)$
- (B)  $c_1 e^x + c_2 e^{-x} + c_3 e^{ix} + c_4 e^{-ix}$
- (C)  $c_1 e^x + c_2 x e^x + c_3 \cos(x) + c_4 \sin(x)$
- (D)  $c_1 e^x + c_2 x e^{-x} + c_3 e^{ix} + c_4 e^{-ix}$

Q.10 Evaluation of  $\iint_S (e^x \hat{i} + 3y \hat{j} - z e^x \hat{k}) \cdot \hat{n} \, dA$  over a surface  $S: x^2 + y^2 + z^2 = 1$ , using Gauss divergence theorem, gives

- (A) 0
- (B)  $4\pi$
- (C)  $4\pi/3$
- (D)  $12\pi$

Q.11 The exact solution of the integral  $\int_0^4 (x^2 - 4) dx$  is denoted by  $I_E$ . The same integral evaluated numerically by the trapezoidal rule and the Simpson's 1/3 rule are denoted by  $I_T$  and  $I_S$ , respectively. The subinterval used in the numerical methods is  $h = 2$ . Then

- (A)  $I_E = I_S > I_T$
- (B)  $I_E = I_S < I_T$
- (C)  $I_E < I_S < I_T$
- (D)  $I_E > I_S > I_T$

**END OF SECTION - A**

## B : FLUID MECHANICS

### Q. 1 – Q. 9 carry one mark each.

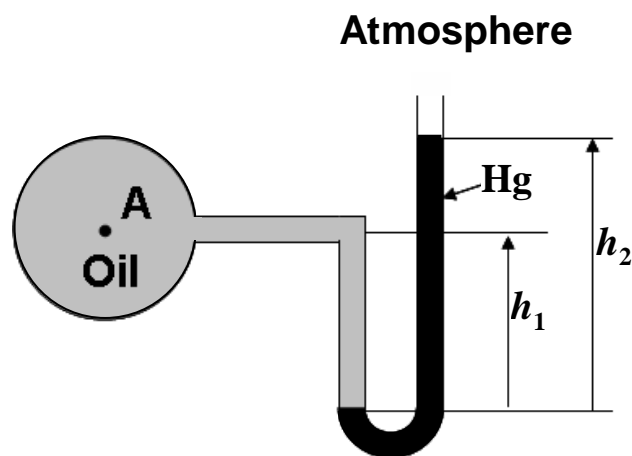
- Q.1 In a two-dimensional flow field, the velocities in the  $x$ - and  $y$ - directions are  $u$  and  $v$ , respectively. The shear stress for a Newtonian fluid having dynamic viscosity  $\mu$  is given by
- (A)  $\mu \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$       (B)  $2\mu \frac{\partial v}{\partial y}$       (C)  $2\mu \frac{\partial u}{\partial x}$       (D)  $\mu \left( \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right)$
- Q.2 In a potential flow, the superposition of the stream functions of a uniform flow and a line source gives rise to a dividing streamline representing
- (A) Rankine's half-body      (B) infinite circular cylinder  
(C) infinite rotating circular cylinder      (D) infinite elliptical cylinder
- Q.3 Given that  $V$ ,  $L$  and  $g$  are the characteristic velocity, characteristic length and acceleration due to gravity, respectively, the expression  $\frac{V}{\sqrt{Lg}}$  represents
- (A) Weber number      (B) Euler number      (C) Cavitation number      (D) Froude number
- Q.4 Match the devices in **Column I** with the characteristics in **Column II**.
- | <b>Column I</b>  | <b>Column II</b>                |
|------------------|---------------------------------|
| P. orifice meter | 1. high head loss and low cost  |
| Q. venturi meter | 2. high head loss and high cost |
|                  | 3. low head loss and high cost  |
|                  | 4. low head loss and low cost   |
- (A) P – 2; Q – 4      (B) P – 1; Q – 2      (C) P – 3; Q – 1      (D) P – 1; Q – 3
- Q.5 Identify the visualization method that shows a PATHLINE in an unsteady flow, assuming that the camera covers the required field of view.
- (A) A dye is continuously injected and a snap shot is taken  
(B) A dye is continuously injected and a long-exposure picture is taken  
(C) A blob (or drop) of dye is injected and a snap shot is taken  
(D) A blob (or drop) of dye is injected and a long-exposure picture is taken
- Q.6 In the case of a fully developed flow through a pipe, the shear stress at the centerline is
- (A) a function of the axial distance      (B) a function of the centerline velocity  
(C) zero      (D) infinite
- Q.7 The velocity in a one-dimensional unsteady flow is given by  $(x^2 - t)$ , where  $x$  is the position and  $t$  is the time. The total acceleration at any  $x$  and  $t$  is
- (A)  $-1 + x t + x^3$       (B)  $-1 + x t + 2 x^3$       (C)  $-1 - x t - x^3$       (D)  $-1 - 2 x t + 2 x^3$
- Q.8 If  $\psi$  is the stream function, the Laplace's equation  $\nabla^2 \psi = 0$  is true when the flow is
- (A) incompressible      (B) incompressible and irrotational  
(C) irrotational      (D) compressible
- Q.9 A fully developed laminar flow is taking place through a pipe. If the flow velocity is doubled maintaining the flow laminar, the pressure loss would be
- (A) halved      (B) unaltered      (C) doubled      (D) trebled

**Q. 10 - Q. 22 carry two marks each.**

Q.10 In the following equations,  $u$  and  $v$  are the velocities in the  $x$ - and  $y$ - directions, respectively and  $t$  is time. The flow field that CANNOT be termed as incompressible is

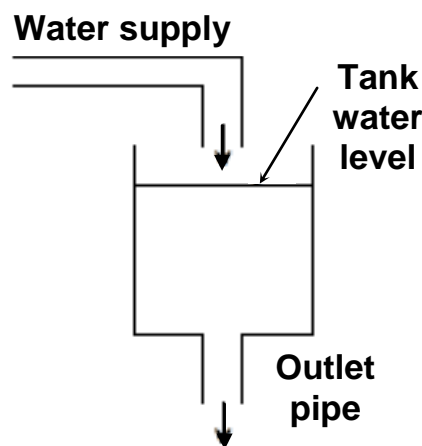
- (A)  $u = x^3 + x y^2, v = y^3 + y x^2$  (B)  $u = 10xt, v = -10yt$   
 (C)  $u = (y/\delta)^{1/7}, v = 0$  ( $\delta = \text{constant}$ ) (D)  $u = 2y, v = 2x$

Q.11 A U-tube mercury (Hg) manometer as shown below is employed to measure the pressure of an oil-filled vessel. The densities of Hg and oil are  $13600 \text{ kg/m}^3$  and  $800 \text{ kg/m}^3$ , respectively. The gravitational acceleration may be taken as  $10 \text{ m/s}^2$ . The gauge pressure (in Pa) at point A when  $h_1 = 0.5 \text{ m}$  and  $h_2 = 0.9 \text{ m}$ , is approximately



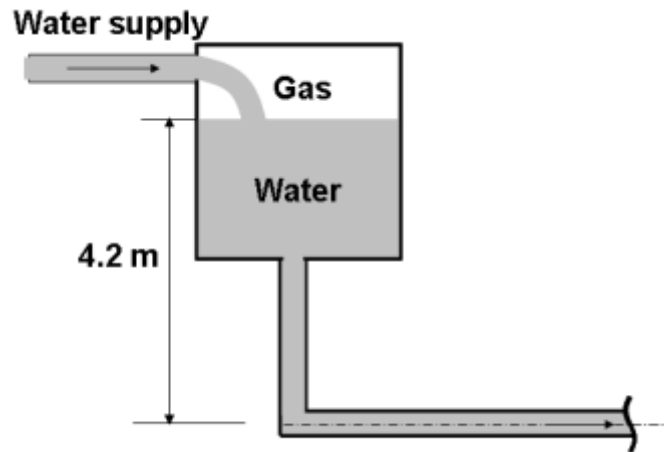
- (A)  $118.4 \times 10^3$  (B) 118.4 (C) 11.84 (D) 1.184

Q.12 Water is supplied to a tank at the rate of  $0.02 \text{ m}^3/\text{s}$ , as shown in the figure below. The cross-sectional area of the tank is  $1 \text{ m}^2$  and the inner diameter of the outlet pipe is  $60 \text{ mm}$ . At a time when the water level in the tank is increasing at the rate of  $5 \text{ mm/s}$ , the average velocity (in  $\text{m/s}$ ) of water in the outlet pipe is approximately

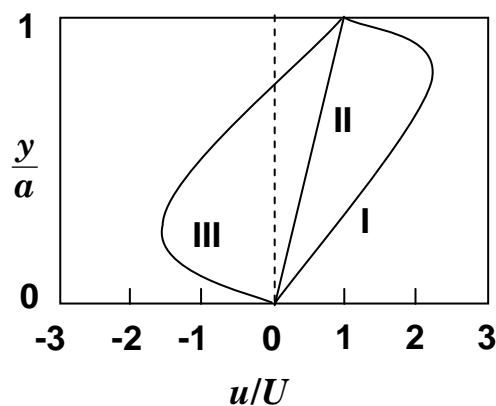


- (A) 0.005 (B) 0.06 (C) 5.3 (D) 20

- Q.13 The water level in a gas-pressurized tank with a large cross-sectional area is maintained constant as shown in the figure below. The water level in the tank is 4.2 m above the pipe centerline as indicated in the figure. The gas pressure is 130 kPa. The atmospheric pressure, gravitational acceleration and density of water may be taken as 100 kPa,  $10 \text{ m/s}^2$  and  $1000 \text{ kg/m}^3$ , respectively. Neglecting losses, the maximum velocity (in m/s) of water at any location in the horizontal portion of the delivery pipe for the pressure NOT to drop below atmospheric pressure, is



- (A) 1.3                      (B) 4.2                      (C) 10                      (D) 12
- Q.14 The figure given below shows typical non-dimensional velocity profiles for fully developed laminar flow between two infinitely long parallel plates separated by a distance  $a$  along  $y$ -direction. The upper plate is moving with a constant velocity  $U$  in the  $x$ -direction and the lower plate is stationary.



Match the non-dimensional velocity profiles in **Column I** with the pressure gradients in **Column II**.

**Column I**

P. profile I

Q. profile II

R. profile III

**Column II**

1.  $\frac{\partial p}{\partial x} > 0$

2.  $\frac{\partial p}{\partial x} < 0$

3.  $\frac{\partial p}{\partial x} = 0$

(A) P - 2; Q - 3; R - 1

(C) P - 3; Q - 1; R - 2

(B) P - 3; Q - 2; R - 1

(D) P - 1; Q - 2; R - 3

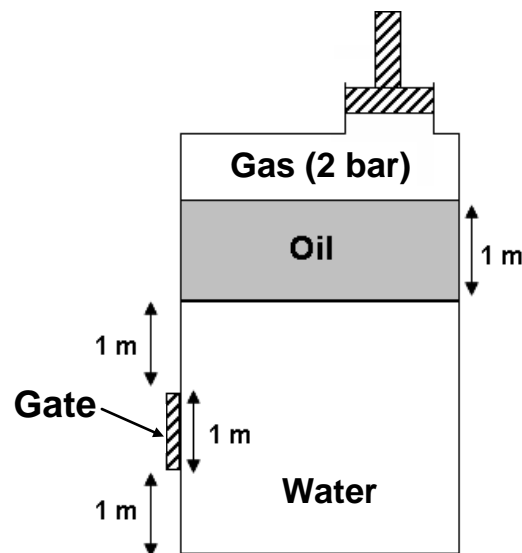


- Q.15 Air flows over a spherical storage vessel of diameter 4 m at a speed of 1 m/s. To find the drag force on the vessel, a test run is to be carried out in water using a sphere of diameter 100 mm. The density and dynamic viscosity of air are  $1.2 \text{ kg/m}^3$  and  $1.8 \times 10^{-5} \text{ Pa}\cdot\text{s}$ , respectively. The density and dynamic viscosity of water are  $1000 \text{ kg/m}^3$  and  $10^{-3} \text{ Pa}\cdot\text{s}$ , respectively. The drag force on the model is 4 N under dynamically similar conditions. The drag force (in N) on the prototype is approximately
- (A) 0.25                      (B) 0.93                      (C) 1.08                      (D) 4
- Q.16 The velocity of an air stream is 20 m/s. The densities of mercury and air are  $13600 \text{ kg/m}^3$  and  $1.2 \text{ kg/m}^3$ , respectively. The gravitational acceleration may be taken as  $10 \text{ m/s}^2$ . When a Pitot-static tube is placed in the stream, assuming the flow to be incompressible and frictionless, the difference between the stagnation and static pressure in the flow field (in mm Hg) would approximately be
- (A) 1760                      (B) 1.76                      (C) 0.57                      (D)  $0.57 \times 10^{-5}$

### Common Data Questions

#### Common Data for Questions 17 and 18:

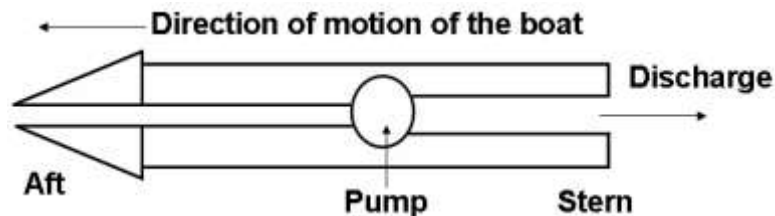
A vessel containing water (density  $1000 \text{ kg/m}^3$ ) and oil (density  $800 \text{ kg/m}^3$ ), pressurized by gas, is shown in the figure below. Assume that the gravitational acceleration is  $10 \text{ m/s}^2$ .



- Q.17 The pressure (in bar) exerted on the bottom wall inside the vessel is approximately
- (A) 0.238                      (B) 2.38                      (C) 23.8                      (D) 238
- Q.18 The gate is 1 m wide perpendicular to the plane of the paper. The force (in N) exerted on the gate is approximately
- (A)  $2.23 \times 10^3$                       (B)  $2.23 \times 10^4$                       (C)  $2.23 \times 10^5$                       (D)  $2.23 \times 10^6$

**Common Data for Questions 19 and 20:**

A boat is propelled in still water at a velocity of 5 m/s by taking water at the rate of  $1 \text{ m}^3/\text{s}$  from the aft side and discharging it through the stern using a pump, as shown in the figure below. The velocity of the discharge jet relative to the boat is 9 m/s. The effect of pressure at the intake and discharge can be neglected. The density of water may be taken as  $1000 \text{ kg/m}^3$ .



- Q.19 The power (in kW) required to propel the boat is  
 (A) 10 (B) 20 (C) 50 (D) 90
- Q.20 The total kinetic energy imparted to the water per second (in kW) by the pump is  
 (A) 10 (B) 25 (C) 28 (D) 81

**Linked Answer Questions****Statement for Linked Answer Questions 21 and 22:**

The hydrodynamic boundary layer over a flat plate is shown in the figure below. The velocity in the  $x$ -direction is approximated as  $u = a + by + cy^2$ , where  $a$ ,  $b$  and  $c$  are constants.  $U$  is the free stream velocity and  $\delta$  is the boundary-layer thickness at any point  $x$  on the plate.



- Q.21 The dimensionless velocity profile is  
 (A)  $\frac{u}{U} = 2 \left( \frac{y}{\delta} \right) - \left( \frac{y}{\delta} \right)^2$  (B)  $\frac{u}{U} = 2 \left( \frac{y}{\delta} \right) + \left( \frac{y}{\delta} \right)^2$   
 (C)  $\frac{u}{U} = 1.5 \left( \frac{y}{\delta} \right) - 0.5 \left( \frac{y}{\delta} \right)^2$  (D)  $\frac{u}{U} = 1.5 \left( \frac{y}{\delta} \right) + 0.5 \left( \frac{y}{\delta} \right)^2$
- Q.22 The displacement thickness (in mm) when  $\delta = 6 \text{ mm}$ , is  
 (A) 2.25 (B) 2 (C) -2 (D) -2.25

**END OF SECTION - B**

**C : MATERIALS SCIENCE**

## Useful data

Boltzmann's constant	: $1.38 \times 10^{-23} \text{ J K}^{-1}$
Charge on an electron	: $1.602 \times 10^{-19} \text{ C}$
Gas Constant	: $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$
Electron rest mass	: $9.1 \times 10^{-31} \text{ kg}$
Permittivity of vacuum ( $\epsilon_0$ )	: $8.854 \times 10^{-12} \text{ F m}^{-1}$
Bohr Magneton	: $9.274 \times 10^{-24} \text{ A/m}^2$

**Q. 1 – Q. 9 carry one mark each.**

- Q.1 Which of the following is **NOT** a Bravais lattice?
- (A) Simple tetragonal  
(B) Body centred tetragonal  
(C) Base centred orthorhombic  
(D) Face centred tetragonal
- Q.2 A Schottky defect in an ionic crystal is a stoichiometric defect of
- (A) Cation vacancy  
(B) Anion vacancy  
(C) Cation and anion vacancy  
(D) Cation and anion interstitial
- Q.3 Which of the following techniques is **NOT** used to grow single crystals of semiconductors?
- (A) Calendering (B) Czochralski (C) Float zone (D) Bridgman
- Q.4 Which of the following signals is produced due to the elastic scattering of electrons by a material?
- (A) Secondary electron  
(B) Backscattered electron  
(C) Auger electron  
(D) Photoelectron
- Q.5 The best magnetostrictive material is
- (A)  $\text{Nd}_2\text{Fe}_{14}\text{B}$  (B)  $\text{Fe}_3\text{O}_4$  (C)  $\text{Cu}_2\text{MnAl}$  (D)  $\text{ZnFe}_2\text{O}_4$
- Q.6 Of the following materials, which is the most suitable for an LED emitting at around 380 nm?
- (A) Direct bandgap material with a small bandgap  
(B) Indirect bandgap material with a large bandgap  
(C) Direct bandgap material with a large bandgap  
(D) Indirect bandgap material with a small bandgap
- Q.7 Which material has the lowest specific heat capacity at room temperature?
- (A) Water (B) Mercury (C) Copper (D) Silver
- Q.8 Microstrain can be measured by X-ray diffraction using peak
- (A) Area and intensity  
(B) Position and area  
(C) Broadening and intensity  
(D) Position and broadening

Q.9 The Pilling-Bedworth ratio is defined as the ratio of

- (A) Volume of oxide to volume of metal
- (B) Weight of oxide to weight of metal
- (C) Density of oxide to density of metal
- (D) Surface area of oxide to surface area of metal

**Q. 10 - Q. 22 carry two marks each.**

Q.10 Match the properties in **Column I** with the appropriate units in **Column II**

<u>Column I</u>	<u>Column II</u>
P. Thermal diffusivity	1. $\text{Hm}^{-1}$
Q. Fracture toughness	2. $\text{m}^2\text{s}^{-1}$
R. Surface energy	3. $\text{Fm}^{-1}$
S. Magnetic permeability	4. $\text{Nm}^{-3/2}$
	5. $\text{Jm}^{-2}$
(A) P-2, Q-5, R-4, S-1	(B) P-2, Q-4, R-5, S-1
(C) P-3, Q-5, R-4, S-3	(D) P-5, Q-4, R-2, S-3

Q.11 Match the characterization techniques in **Column I** with the options in **Column II**

<u>Column I</u>	<u>Column II</u>
P. Scanning tunneling microscopy	1. No vacuum required
Q. Scanning electron microscopy	2. Backscattered electrons
R. Transmission electron microscopy	3. Photoelectrons
S. Atomic force microscopy	4. Atomically sharp tip
	5. Sub-Angstrom resolution
(A) P-4, Q-2, R-5, S-1	(B) P-1, Q-3, R-4, S-5
(C) P-2, Q-4, R-1, S-5	(D) P-5, Q-1, R-2, S-4

Q.12 Match the materials in **Column I** with the applications in **Column II**

<u>Column I</u>	<u>Column II</u>
P. Titanium diboride	1. Photocatalyst
Q. Molybdenum disilicide	2. Furnace heating element
R. Hydroxyapatite	3. Ultra high temperature material
S. Nanocrystalline titanium oxide	4. Tough ceramic
	5. Artificial bone implant
(A) P-3, Q-4, R-5, S-1	(B) P-5, Q-3, R-2, S-1
(C) P-4, Q-3, R-1, S-5	(D) P-3, Q-2, R-5, S-1

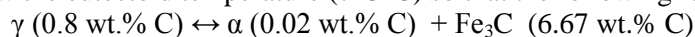
Q.13 Match the properties in **Column I** with the options in **Column II**

<u>Column I</u>	<u>Column II</u>
P. Toughness	1. Resistance to plastic deformation
Q. Resilience	2. Time dependent permanent deformation under constant load
R. Creep	3. Total elongation at failure
S. Hardness	4. Area under the stress-strain curve
	5. Area under the elastic part of the stress-strain curve
(A) P-5, Q-1, R-3, S-2	(B) P-4, Q-3, R-2, S-1
(C) P-4, Q-5, R-2, S-1	(D) P-5, Q-4, R-3, S-2

- Q.14 Determine the mole fraction of vinyl chloride in a copolymer of vinyl chloride ( $\text{CH}_2\text{CHCl}$ ) and vinyl acetate ( $\text{CH}_2\text{-CH-OCOCH}_3$ ) having molecular weight of 10520 g/mol and degree of polymerization of 160.
- (A) 0.14                      (B) 0.30                      (C) 0.70                      (D) 0.86
- Q.15 The electron concentration in an n-type semiconductor is  $5 \times 10^{18}/\text{m}^3$ . If the drift velocity of electrons is 100 m/s in an electric field of 500 V/m, calculate the conductivity of the semiconductor.
- (A)  $0.16 \times 10^{-1} \text{ S/m}$     (B)  $1.60 \times 10^{-1} \text{ S/m}$     (C)  $2.50 \times 10^{-1} \text{ S/m}$     (D)  $30.05 \times 10^{-1} \text{ S/m}$
- Q.16 Calculate the saturation magnetization ( $M_{\text{sat}}$ ) for bcc iron of lattice parameter 2.866 Å.
- (A)  $0.79 \times 10^6 \text{ A/m}$     (B)  $1.5 \times 10^6 \text{ A/m}$     (C)  $3.15 \times 10^6 \text{ A/m}$     (D)  $4.73 \times 10^6 \text{ A/m}$

### Common Data Questions

**Common Data for Questions 17 and 18:** A plain 0.45 wt.% carbon steel is cooled slowly from 900°C to just below the eutectoid temperature (723°C) so that the following reaction occurs:



- Q.17 During cooling from 900°C to 723°C, the proeutectoid  $\alpha$  forms from  $\gamma$ . Find the volume % of proeutectoid  $\alpha$  just below 723°C for the steel.
- (A) 44.9%                      (B) 66.1%                      (C) 55.1%                      (D) 34.9%
- Q.18 Find the volume % of pearlite for the steel just below 723°C for 0.45 wt.% carbon steel.
- (A) 44.9%                      (B) 55.1%                      (C) 40.9%                      (D) 59.1%

**Common Data for Questions 19 and 20:** A 20 kN tensile load is applied axially to a steel bar of cross-sectional area 8 cm<sup>2</sup> and 1m length. The Young's modulus of steel ( $E_{\text{steel}}$ ) is 200 GPa, and of aluminium ( $E_{\text{Al}}$ ) is 70 GPa. The Poisson's ratio ( $\nu$ ) can be taken as 0.3.

- Q.19 When the same load is applied to an aluminium bar, it is found to give same elastic strain as the steel. Calculate the cross-sectional area of the aluminium bar.
- (A) 11.43 cm<sup>2</sup>                      (B) 14.93 cm<sup>2</sup>                      (C) 18.26 cm<sup>2</sup>                      (D) 22.86 cm<sup>2</sup>
- Q.20 Calculate the final area of the steel bar after the deformation under the applied load of 20 kN.
- (A) 7.9 cm<sup>2</sup>                      (B) 9.7 cm<sup>2</sup>                      (C) 7.0 cm<sup>2</sup>                      (D) 8.1 cm<sup>2</sup>

### Linked Answer Questions

**Statement for Linked Answer Questions 21 and 22:** Chromium has the bcc structure with atomic diameter of 2.494 Å.

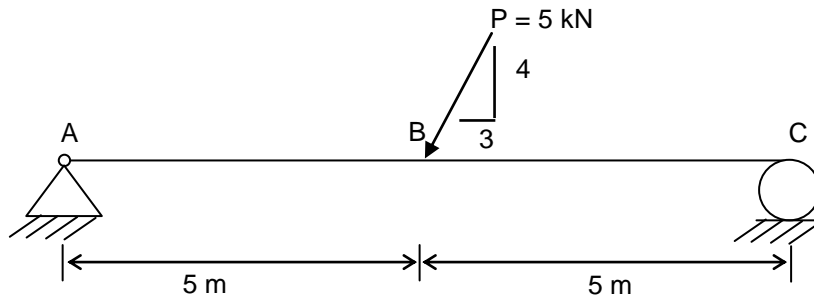
- Q.21 Calculate the lattice parameter of chromium assuming tight atomic bonding.
- (A) 1.442 Å                      (B) 2.880 Å                      (C) 4.323 Å                      (D) 5.764 Å
- Q.22 Find the first diffraction peak position ( $2\theta$ ) for Cu  $K\alpha$  radiation with a wavelength of 1.54 Å
- (A) 21.76°                      (B) 33.05°                      (C) 44.43°                      (D) 66.10°

**END OF SECTION - C**

### D : SOLID MECHANICS

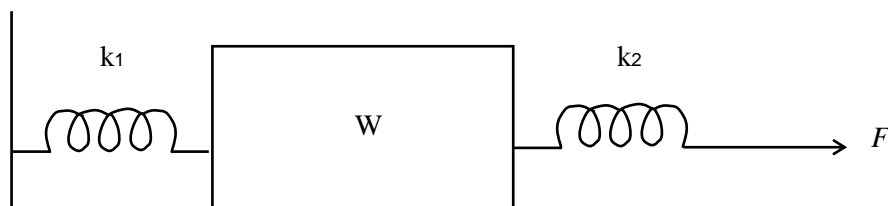
**Q. 1 – Q. 9 carry one mark each.**

Q.1 The axial force diagram for the weightless beam subjected to the inclined force  $P = 5 \text{ kN}$  is



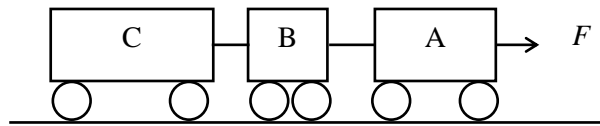
- (A)
- (B)
- (C)
- (D)

Q.2 A block of weight  $W$ , connected to two springs with spring constants  $k_1$  and  $k_2$ , rests initially on a horizontal frictional surface. The coefficient of static friction between the block and the surface is  $\mu$ . Both springs are initially undeformed. The magnitude of force  $F$ , applied to the second spring, is now gradually increased. The block will start to slide when  $F$  becomes

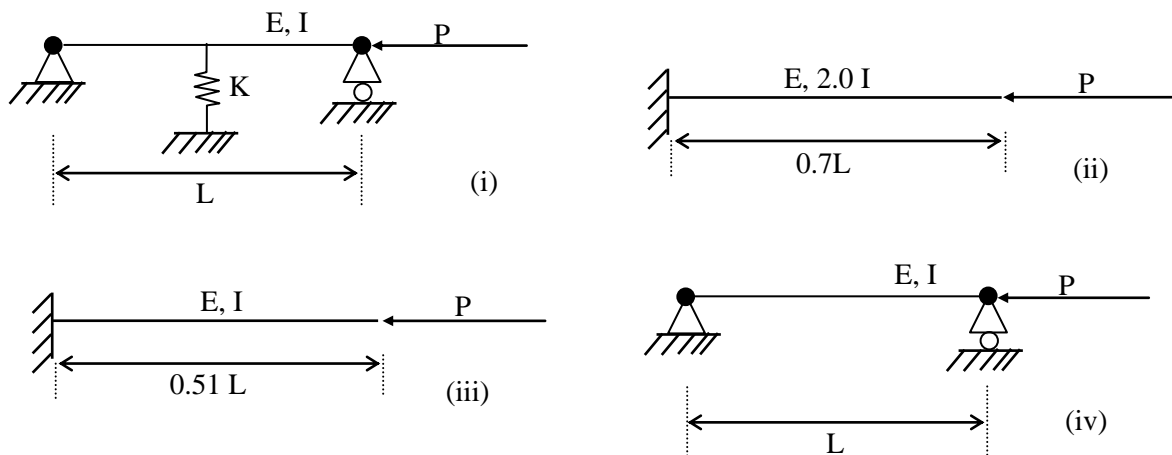


- (A)  $\mu W$  (B)  $k_1 \mu W / (k_1 + k_2)$   
 (C)  $k_2 \mu W / (k_1 + k_2)$  (D)  $k_2 \mu W / k_1$

- Q.3 Three connected railway coaches A, B and C of masses  $m_A$ ,  $m_B$  and  $m_C$ , respectively are being pulled by a locomotive with force  $F$  over a horizontal track. The coaches may be assumed to move on frictionless wheels with negligible air resistance. The tension in the connector between coaches A and B is



- (A)  $F$  (B)  $Fm_A/(m_A + m_B + m_C)$   
 (C)  $Fm_B/(m_A + m_B + m_C)$  (D)  $F(m_B + m_C)/(m_A + m_B + m_C)$
- Q.4 For the beam-column configurations shown in figure, the minimum Euler buckling load is obtained for the case (Young's modulus and second moment of cross-sectional area are as indicated)



- (A) (i) (B) (ii) (C) (iii) (D) (iv)
- Q.5 A disk of mass  $m = 0.25 \text{ g}$  and radius  $r = 10 \text{ mm}$  is at rest relative to a mass-less horizontal turntable spinning about a vertical axis at an angular speed of  $\omega = 2 \text{ rad/s}$ . The turntable is assumed to be mounted on frictionless bearings. Another identical, initially non-rotating disk is dropped onto the spinning disk. Friction causes both disks (and the turntable) to eventually rotate at the same angular speed. The eventual angular speed of the disks is

- (A) 0.15 rad/s (B) 1 rad/s (C) 2 rad/s (D) 4 rad/s

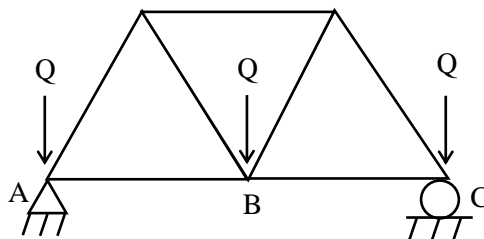
- Q.6 A rocket in the atmosphere is accelerating upwards with acceleration  $a \text{ m/s}^2$ . The natural frequency of a spring-mass system (with mass  $m \text{ kg}$  and spring constant  $k \text{ N/m}$ ), suspended vertically inside the rocket, is (take  $g \text{ m/s}^2$  to be the acceleration due to gravity)

- (A)  $\sqrt{\frac{k}{m}}$ ; ( $\bar{k} < k$ ) (B)  $\sqrt{\frac{k}{m}}$  (C)  $\sqrt{\frac{kg}{ma}}$  (D)  $\sqrt{\frac{k}{m}(1 - \frac{a}{g})}$

- Q.7 An irregular planar body in space is acted upon by a force  $\vec{F} = (2\vec{i} + \vec{j})N$  at position  $\vec{r}_1 = (\vec{i} + 2\vec{j})m$  and a moment  $\vec{M} = 3\vec{k}Nm$  at position  $\vec{r}_2 = (-2\vec{i})m$ . The corresponding equivalent force  $\vec{F}_o$  and moment  $\vec{M}_o$  at the origin are
- (A)  $\vec{F}_o = (2\vec{i} + \vec{j})N; \vec{M}_o = (3\vec{k})Nm$   
 (B)  $\vec{F}_o = (2\vec{i} + \vec{j})N; \vec{M}_o = 0Nm$   
 (C)  $\vec{F}_o = (-2\vec{i} - \vec{j})N; \vec{M}_o = (-6\vec{k})Nm$   
 (D)  $\vec{F}_o = (2\vec{i} + \vec{j})N; \vec{M}_o = (6\vec{k})Nm$
- Q.8 A hollow shaft and a solid shaft constructed of the same material have the same length and the same outer radius  $R$ . The inner radius of the hollow shaft is  $0.6R$ . Assuming that both shafts are subjected to the same torque, the ratio of the maximum shear stress in the hollow shaft to that in the solid shaft is
- (A) 1.1                      (B) 1.2                      (C) 1.15                      (D) 0.95
- Q.9 A point in a beam experiences a tensile stress (due to bending) of  $50 \text{ N/mm}^2$  and a shear stress of  $20 \text{ N/mm}^2$ . The principal stresses are
- (A)  $17 \text{ N/mm}^2$  tension,  $67 \text{ N/mm}^2$  compression  
 (B) 0, 0  
 (C)  $57 \text{ N/mm}^2$  tension,  $7 \text{ N/mm}^2$  compression  
 (D)  $52 \text{ N/mm}^2$  compression,  $15 \text{ N/mm}^2$  tension

**Q. 10 - Q. 22 carry two marks each.**

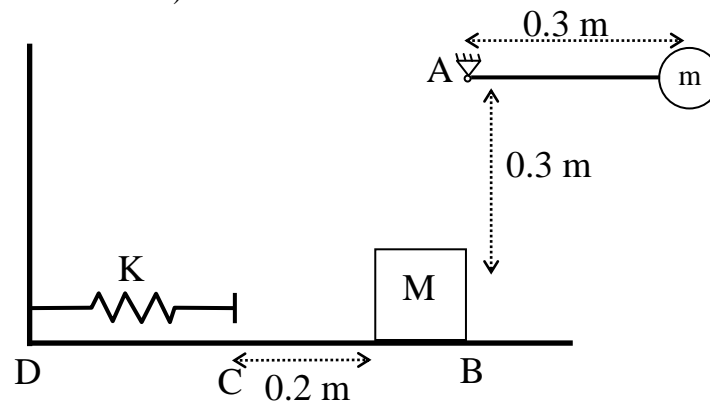
- Q.10 Consider a simply supported beam loaded either by a uniformly distributed transverse load or by a concentrated transverse load applied at the center such that the maximum bending stress in both cases is the same. The ratio of the strain energy for the two cases is
- (A) 4/5                      (B) 5/8                      (C) 8/5                      (D) 1
- Q.11 A small railway bridge is constructed from identical steel truss members, each of length  $l$ , cross-sectional area  $A$  and Young's modulus  $E$ . A train stops on the bridge. The loads applied by the train on the truss on one side of the bridge may be assumed to act at pins A, B and C, as shown. The displacement of the support C due to this loading is



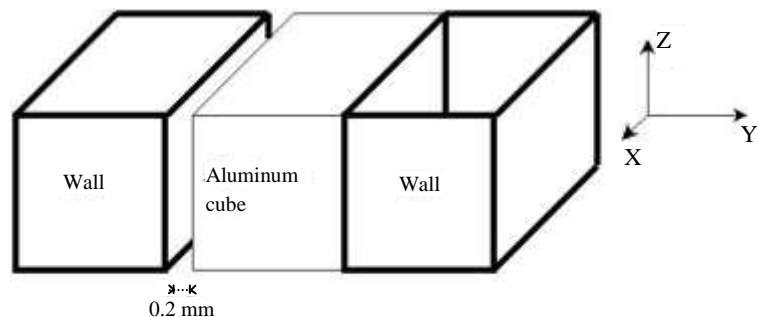
- (A) 0    (B)  $Ql/(AE)$   
 (C)  $\sqrt{3}Ql/(4AE)$     (D)  $Ql/(\sqrt{3}AE)$
- Q.12 A vertical pole, cantilevered at the bottom, has a solid circular cross-section of diameter  $d = 49.21 \text{ mm}$ . It is loaded by a horizontal force  $P = 6675 \text{ N}$  at the top end. The maximum shear stress in the pole is
- (A)  $4.25 \text{ N/mm}^2$                       (B)  $5.68 \text{ N/mm}^2$                       (C)  $4.68 \text{ N/mm}^2$                       (D)  $7.50 \text{ N/mm}^2$



- Q.13 A striker with mass  $m=20$  kg is attached to the end of a mass-less rigid bar of length  $R=0.3$ m. The bar is hinged to support A, and swings down from an initial horizontal position such that the striker hits mass  $M= 5$ kg elastically. The mass  $M$  slides (in a straight line) along the table, from point B towards the spring located at point C, 0.2 m away from B. Assume that the coefficient of friction in the region BC is  $\mu_d = 0.4$ ; the region CD frictionless. Let the spring constant of the spring be  $k = 4000$  N/m. If the striker rises to a maximum height of 0.1m below its starting location, then the maximum compression of the spring is (let acceleration due to gravity  $g = 10$  m/s<sup>2</sup>, the dimensions of the striker and mass are small)

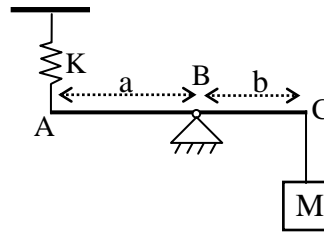


- (A) 0.000 m      (B) 0.100 m      (C) 0.089 m      (D) 0.109 m
- Q.14 A cube, made of aluminum, of dimension  $0.1$  m  $\times$   $0.1$  m  $\times$   $0.1$  m, rests against a rigid wall (with normal in the  $y$ -direction), as shown in the figure. Another parallel rigid wall is located at a clearance of 0.2 mm from the block. Assuming all contacts to be frictionless, if the block is heated by  $\Delta T = 150^\circ\text{C}$ , the normal stress  $\sigma_{yy}$  induced in the block is (for aluminum  $E = 70$  GPa;  $\nu = 0.3$ ;  $\alpha = 20 \times 10^{-6} / ^\circ\text{C}$ )



- (A)  $\sigma_{yy} = -7$  MPa  
 (B)  $\sigma_{yy} = 7$  MPa  
 (C)  $\sigma_{yy} = -70$  MPa  
 (D)  $\sigma_{yy} = 0$
- Q.15 A thin walled spherical pressure vessel made of a linear elastic isotropic material has inner radius  $r$  and thickness  $t$  before pressurization. When subjected to internal pressure  $p$ , elements of the pressure vessel wall experience a state of stress described by a single point  $(\sigma, \tau) = (pr/(2t), 0)$  in Mohr's circle. The reduction of the wall thickness due to pressurization
- (A) increases with  $t$   
 (B) remains independent of  $t$   
 (C) decreases with  $t$   
 (D) depends on the elastic properties.

- Q.16 For small oscillations, the natural frequency of the system in terms of  $K$ ,  $a$ ,  $b$  and  $M$  is (assuming ideal joints and mass-less rigid rod ABC)



- (A)  $\sqrt{\frac{K}{M}}$       (B)  $\sqrt{\frac{Ka}{Mb}}$       (C)  $\sqrt{\frac{Kb^2}{Ma^2}}$       (D)  $\sqrt{\frac{Ka^2}{Mb^2}}$

### Common Data Questions

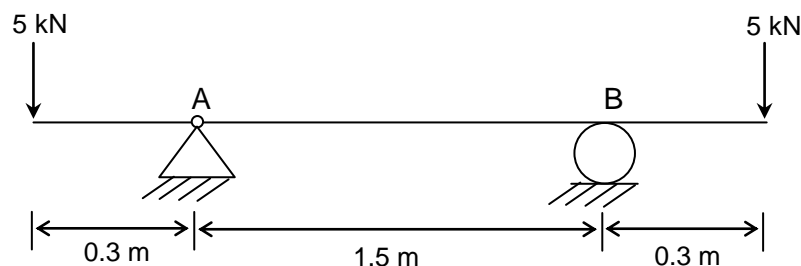
#### Common Data for Questions 17 and 18:

A steel cylindrical pressure vessel has an inner radius of 1.8 m and a wall thickness of 20 mm.

- Q.17 For an internal pressure of 800 kPa the maximum shear stress for the cylindrical part of the vessel is  
 (A) 16 MPa      (B) 18 MPa      (C) 20 MPa      (D) 0
- Q.18 At which of the following internal pressures will the cylindrical vessel yield as per the Tresca criterion if the yield strength of the material in tension is 320 MPa  
 (A) 3.55 MPa      (B) 7.1 MPa      (C) 1.775 MPa      (D) 4.0 MPa

#### Common Data for Questions 19 and 20:

A steel beam, of rectangular cross-section 25 mm wide and 75 mm deep, is pinned to supports at points A and B, where the support B is on rollers. The Young's modulus of steel may be assumed as  $2.0 \times 10^5 \text{ N/mm}^2$ . The ends of the beam are loaded with 5 kN loads.

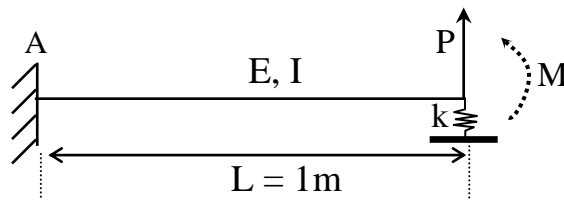


- Q.19 The maximum bending stress in the beam is  
 (A) 0      (B) 64 MN/m<sup>2</sup>      (C) 128 MN/m<sup>2</sup>      (D) 32 MN/m<sup>2</sup>
- Q.20 The vertical deflection at the ends is  
 (A) 4.92 mm      (B) 4.58 mm      (C) 9.31 mm      (D) 9.84 mm

## Linked Answer Questions

### Statement for Linked Answer Questions 21 and 22:

A cantilevered beam of unknown material (which is homogeneous, linearly elastic and isotropic) and an unknown cross-section (which is uniform and symmetric) is given in the figure. The stiffness of the end spring is  $k = 2000 \text{ N/m}$  and end load  $P = 1000 \text{ N}$ ; length of the beam  $L = 1 \text{ m}$ .



- Q.21 If the deflection at the free-end (under load  $P$ , with end moment  $M=0$ ) is measured as  $\delta = 5 \text{ mm}$ , the flexural rigidity  $EI$  for the beam is (in  $\text{N m}^2$ )
- (A) 66,666                      (B) 66,000                      (C) 67,300                      (D) 64,000
- Q.22 The value of the additional end moment  $M$  (in  $\text{N.m}$ ) required to obtain an upward deflection of  $1 \text{ mm}$  at the free end, is (moment is positive in counterclockwise direction)
- (A)  $-533.33$                       (B)  $533.33$                       (C)  $-528$                       (D)  $528$

**END OF SECTION - D**

## E : THERMODYNAMICS

**Note:** Usual notations have been used for thermodynamic variables.

**Useful Data:**

Unless otherwise specified, the following data may be assumed.

Universal gas constant,  $\bar{R} = 8.314 \text{ kJ/kmol.K}$ ; Acceleration due to gravity,  $g = 9.81 \text{ m/s}^2$

Molecular mass of air,  $M_{air} = 29 \text{ kg/kmol}$ ; Specific heat of air at constant pressure,  $c_p = 1.005 \text{ kJ/kg.K}$

Ratio of specific heats of air,  $\gamma = 1.4$ . Assume air to be a perfect gas unless specified otherwise.

**Q. 1 – Q. 9 carry one mark each.**

Q.1 Consider a piston-cylinder arrangement containing a gas. This system is heated by placing it on the top of a burner. The system undergoes

- (A) a constant volume process
- (B) a constant pressure process
- (C) an adiabatic process
- (D) an isothermal process

Q.2 For a pure substance, at the triple point

- (A) only solid and liquid phases co-exist in equilibrium
- (B) only liquid and vapour phases co-exist in equilibrium
- (C) only solid and vapour phases co-exist in equilibrium
- (D) solid, liquid and vapour phases co-exist in equilibrium

Q.3 In a saturated liquid-vapour mixture, the property quality,  $x$  is defined as

- |  |   |
|--|---|
| (A) $x = \frac{m_{vapour}}{m_{liquid} + m_{vapour}}$ | (B) $x = \frac{m_{vapour}}{m_{liquid}}$ |
| (C) $x = \frac{m_{liquid}}{m_{liquid} + m_{vapour}}$ | (D) $x = \frac{m_{liquid}}{m_{vapour}}$ |

Q.4 The slope of a Mollier diagram at constant pressure indicates

- |                     |                 |
|---------------------|-----------------|
| (A) enthalpy        | (B) entropy     |
| (C) internal energy | (D) temperature |

Q.5 If  $Q_L$  represents the magnitude of heat transfer from a low temperature reservoir to a cyclic device and  $Q_H$  represents the magnitude of heat transfer from a cyclic device to a high temperature reservoir, then for the same  $Q_L$  and  $Q_H$ , the coefficient performance of a refrigerator ( $COP_R$ ) and the coefficient performance of a heat pump ( $COP_{HP}$ ) can be related as

- |                                |                            |
|--------------------------------|----------------------------|
| (A) $COP_R = 1 - COP_{HP}$     | (B) $COP_{HP} = COP_R + 1$ |
| (C) $COP_R \cdot COP_{HP} = 1$ | (D) $COP_{HP} = COP_R - 1$ |

Q.6 Clausius inequality is written as

- |                                       |                                    |
|---------------------------------------|------------------------------------|
| (A) $\oint \delta Q > 0$              | (B) $\oint \delta Q < 0$           |
| (C) $\oint \frac{\delta Q}{T} \leq 0$ | (D) $\oint \frac{\delta Q}{T} > 0$ |

- Q.7 In a Diesel cycle, the ratio of cylinder volumes after and before combustion process is called  
 (A) cut-off ratio (B) back work ratio (C) pressure ratio (D) compression ratio
- Q.8 The exergy (or availability) of a system at a specified state  
 (A) depends on the conditions of the system alone  
 (B) depends on the conditions of the environment alone  
 (C) depends on the conditions of both the system and environment  
 (D) depends neither on the conditions of the system nor the environment
- Q.9 In each of the following choices, there are two expressions given. Select the choice that gives, first, the defining expression of volume expansivity and second, the expression of volume expansivity for ideal gases
- (A)  $\frac{1}{v} \left( \frac{\partial v}{\partial T} \right)_p, \frac{1}{T}$  (B)  $\frac{1}{v} \left( \frac{\partial v}{\partial P} \right)_T, \frac{1}{T}$   
 (C)  $-\frac{1}{v} \left( \frac{\partial v}{\partial P} \right)_T, \frac{1}{P}$  (D)  $\frac{1}{v} \left( \frac{\partial v}{\partial T} \right)_p, \frac{1}{P}$

**Q. 10 - Q. 22 carry two marks each.**

- Q.10 A certain mass of gas at 0°C is expanded to 81 times its original volume under adiabatic conditions. If ratio of specific heats of the gas,  $\gamma = 1.25$ , the final temperature of the gas is  
 (A) -235 °C (B) -182 °C (C) -91 °C (D) 0 °C
- Q.11 A sample of gas with initial average kinetic energy,  $E$  is heated from 27 °C to 327 °C. The average kinetic energy after heating is  
 (A)  $E$  (B)  $2E$  (C)  $27E$  (D)  $327E$
- Q.12 Helium in a piston/cylinder assembly at 20°C and 100 kPa is brought to 400 K in a reversible polytropic process with exponent  $n = 1.25$ . Assume helium to be an ideal gas. The molecular mass of helium is 4.003 kg/kmol. The specific work in the process is approximately  
 (A) -800 kJ/kg (B) -788 kJ/kg (C) 788 kJ/kg (D) -888 kJ/kg
- Q.13 32 kg of oxygen is mixed with 28 kg of nitrogen at the same temperature. The gases are at the same pressure of 103 kPa before and after mixing. If  $\bar{R}$  is the universal gas constant in kJ/kmol.K, the change in entropy of the mixture is  
 (A)  $1.38\bar{R}$  (B)  $0.69\bar{R}$  (C)  $\bar{R}$  (D)  $0.34\bar{R}$
- Q.14 Consider two Carnot heat engines A and B operating in series. Engine A receives heat from a reservoir at 1750 K and rejects heat to another reservoir at temperature  $T$ . Engine B receives an amount of energy same as that rejected by Engine A from the reservoir at temperature  $T$ . Engine B then rejects heat to another reservoir at 320 K. In both cases, the engines produce some amount of work. If the thermal efficiencies of both the engines are the same, then the temperature  $T$  is approximately  
 (A) 848 K (B) 748 K (C) 648 K (D) 548 K

Q.15 Joule-Thomson coefficient for a gas,  $\mu_j$  obeying the relation  $p(v-b)=RT$  is

(A)  $\mu_j = \frac{c_p}{b}$       (B)  $\mu_j = \frac{b}{c_p}$       (C)  $\mu_j = -\frac{b}{c_p}$       (D)  $\mu_j = -\frac{c_p}{b}$

Q.16 The correct expression representing  $Z$  to be a thermodynamic property is

(A)  $Z = pdv$   
 (B)  $Z = vdp$   
 (C)  $Z = pdv + vdp$   
 (D)  $Z = pdv - vdp$

### Common Data Questions

#### Common Data for Questions 17 and 18:

The vapour pressure of liquid ammonia (in atmosphere) in the vicinity of the triple point can be expressed as

$$\ln p + \frac{3063}{T} = 15.16$$

where temperature  $T$  is expressed in K.

In a similar manner, the vapour pressure of solid ammonia can be expressed as

$$\ln p + \frac{3754}{T} = 18.7$$

Take the molecular mass of ammonia to be 17 kg/kmol.

Q.17 The temperature and pressure at the triple point are

(A) 295.2 K, 0.69 atm      (B) 295.2 K, 0.59 atm  
 (C) 195.2 K, 0.69 atm      (D) 195.2 K, 0.59 atm

Q.18 The latent heat of vapourization is

(A) 1298 kJ/kg      (B) 1398 kJ/kg      (C) 1498 kJ/kg      (D) 1698 kJ/kg

#### Common Data for Questions 19 and 20:

Consider an ideal reheat cycle utilizing steam. Steam leaves the boiler and enters the turbine at 3 MPa, 400°C (state 3) and then expands to 0.8 MPa (state 4). It is then reheated at constant pressure 0.8 MPa to 400°C (state 5) and expands to 10 kPa in the low pressure turbine (state 6). The entry to the pump corresponds to saturated liquid state (state 1), and state 2 represents inlet to the boiler. The following data are given:

$$h_1 = 191.81 \text{ kJ/kg}, h_3 = 3230.82 \text{ kJ/kg}, h_4 = 2891.6 \text{ kJ/kg}, h_5 = 3267.97 \text{ kJ/kg},$$

$$h_g|_{10 \text{ kPa}} = 2584.63 \text{ kJ/kg}, x_6 = 0.92285, v_f|_{10 \text{ kPa}} = 0.00101 \text{ m}^3/\text{kg}$$

Q.19 The heat transfer in the boiler is approximately

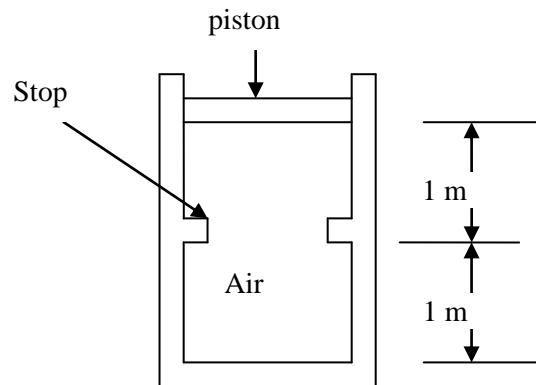
(A) 4411 kJ/kg      (B) 3412 kJ/kg  
 (C) 3230 kJ/kg      (D) 2892 kJ/kg

Q.20 The net workdone in the cycle is approximately

(A) 1004 kJ/kg      (B) 1104 kJ/kg  
 (C) 1204 kJ/kg      (D) 2004 kJ/kg

**Linked Answer Questions****Statement for Linked Answer Questions 21 and 22:**

A piston-cylinder arrangement as shown in the figure initially contains air at 150 kPa and 400°C. The arrangement is allowed to cool to the ambient temperature of 20°C. The characteristic gas constant for air is 0.287 kJ/kg.K. The cylinder wall has stops of negligible thickness that can prevent the piston from moving down. The stops are 1 m from the inner side of the base surface of the cylinder. At the initial state, the piston is resting 1 m above the stops.



Q.21 The final pressure in the cylinder is

- (A) 130.7 kPa (B) 150 kPa  
(C) 200.7 kPa (D) 230.7 kPa

Q.22 The specific work done by the air during the process is

- (A) -26.67 kJ/kg (B) 26.67 kJ/kg  
(C) 49.5 kJ/kg (D) -96.67 kJ/kg

**END OF SECTION - E**

**F : POLYMER SCIENCE AND ENGINEERING****Q. 1 – Q. 9 carry one mark each.**

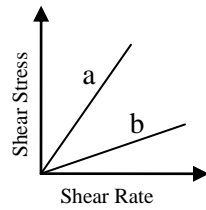
- Q.1 The diamine used for the synthesis of nylon 6,4 is  
(A) tetramethylene diamine (B) hexamethylene diamine  
(C) phenylene diamine (D) cyclohexane-1,4-diamine
- Q.2 A small amount of hydroquinone is added to methyl methacrylate monomer in order to  
(A) improve its thermal stability  
(B) improve its hydrolytic stability  
(C) inhibit polymerization  
(D) regulate molecular weight
- Q.3 Which of the following compounds is used in Zeigler-Natta catalyst?  
(A)  $\text{TiCl}_3$  (B)  $\text{CaCl}_2$   
(C)  $\text{ZnCl}_2$  (D)  $\text{NaCl}$
- Q.4 The z-average molecular weight,  $\overline{M}_z$  can be estimated using  
(A) End group analysis (B) Osmometry  
(C) Viscometry (D) Ultracentrifugation
- Q.5 The unit of intrinsic viscosity is  
(A) dl/g (B) g/dl (C) poise (D) g/mol
- Q.6 Heat dissipation is most inefficient in  
(A) Emulsion polymerization (B) Solution polymerization  
(C) Bulk polymerization (D) Suspension polymerization
- Q.7 The crystalline melting temperature of the polymers high density polyethylene (HDPE), isotactic polypropylene (iPP), nylon 6 (PA6) and poly(ethylene terephthalate) (PET) can be arranged as  
(A)  $T_{\text{HDPE}} > T_{\text{PET}} > T_{\text{iPP}} > T_{\text{PA6}}$   
(B)  $T_{\text{PET}} > T_{\text{PA6}} > T_{\text{iPP}} > T_{\text{HDPE}}$   
(C)  $T_{\text{PA6}} > T_{\text{HDPE}} > T_{\text{PET}} > T_{\text{iPP}}$   
(D)  $T_{\text{iPP}} > T_{\text{PA6}} > T_{\text{PET}} > T_{\text{HDPE}}$
- Q.8 Which of the following polymers is sensitive to moisture absorption?  
(A) Polyethylene (B) Polystyrene (C) Polyamide 6 (D) Polybutadiene
- Q.9 Most engineering polymers have heat distortion temperature (HDT) in excess of  
(A)  $-80^\circ\text{C}$  (B)  $0^\circ\text{C}$  (C)  $20^\circ\text{C}$  (D)  $80^\circ\text{C}$

**Q. 10 - Q. 22 carry two marks each.**

- Q.10 Two miscible polymers A and B are blended in weight ratio of 30:70. If the glass transition temperature,  $T_g$  of polymer A is  $-50^\circ\text{C}$  and that of polymer B is  $100^\circ\text{C}$ , then the  $T_g$  of the blend is  
(A)  $-10.5^\circ\text{C}$  (B)  $25.0^\circ\text{C}$  (C)  $37.5^\circ\text{C}$  (D)  $74.8^\circ\text{C}$

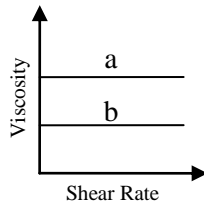


Q.11 If the flow curves of two viscous fluids are represented by

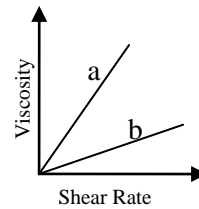


then, the viscosity plots of the fluids will be

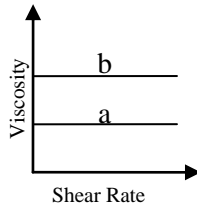
(A)



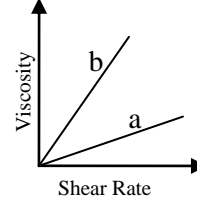
(B)



(C)



(D)



Q.12 Match the following **compounding ingredients** in plastic technology with their respective **functions**:

**Compounding ingredients**

- P. Tricresyl phosphate  
Q. Calcium carbonate  
R. Azodicarbonamide  
S. *o*-Hydroxybenzophenone

**Functions**

1. Filler  
2. UV stabilizer  
3. Plasticizer  
4. Blowing agent

(A) P-3, Q-1, R-4, S-2

(B) P-1, Q-4, R-3, S-2

(C) P-4, Q-1, R-2, S-3

(D) P-3, Q-4, R-1, S-2

Q.13 In a three-point bending mode for flexural test of a polymer sample with the following data:

- load applied in the mid-span = 80 kg  
width of the specimen = 3 cm  
depth of the specimen = 2 cm  
length of the specimen = 30 cm

the flexural strength will be

(A) 17.5 MPa

(B) 29.4 MPa

(C) 35.7 MPa

(D) 41.3 MPa

Q.14 How many stereo isomers are possible in total on polymerization of butadiene?

(A) 2

(B) 3

(C) 4

(D) 5

Q.15 Match the following **processing operations** with their respective **tools**:

<b>Processing operations</b>	<b>Tools</b>
P. Injection molding	1. Parison mold
Q. Twin screw extrusion	2. Sprue-runner system
R. Blow molding	3. Mixing head
S. Reaction injection molding	4. Kneading blocks

(A) P-1, Q-2, R-3, S-4

(B) P-2, Q-4, R-1, S-3

(C) P-2, Q-1, R-4, S-3

(D) P-4, Q-1, R-2, S-3

Q.16 If a solid elastomer ball of weight 100 g is allowed to free fall from a height of 10 m and it rebounds back to a height of 8 m, the hysteresis loss is

(A) 19.60 J

(B) 9.80 J

(C) 1.96 J

(D) 0.98 J

### Common Data Questions

#### Common Data for Questions 17 and 18:

A polymer mixture contains three monodisperse polystyrene samples A, B and C of molecular weights 10000, 20000 and 30000 g mol<sup>-1</sup>, respectively.

Q.17 If the mixture contains equal number of molecules of A, B and C, the weight average molecular weight,  $\overline{M}_w$  will be

(A)  $1.93 \times 10^4$  g mol<sup>-1</sup>

(B)  $2.13 \times 10^4$  g mol<sup>-1</sup>

(C)  $2.33 \times 10^4$  g mol<sup>-1</sup>

(D)  $2.53 \times 10^4$  g mol<sup>-1</sup>

Q.18 If the mixture contains equal masses of A, B and C, then the number average molecular weight,  $\overline{M}_n$  will be

(A)  $1.64 \times 10^4$  g mol<sup>-1</sup>

(B)  $1.74 \times 10^4$  g mol<sup>-1</sup>

(C)  $1.84 \times 10^4$  g mol<sup>-1</sup>

(D)  $1.94 \times 10^4$  g mol<sup>-1</sup>

#### Common Data for Questions 19 and 20:

The stress relaxation equation for polymers is given by,  $\sigma = \sigma_0 e^{-t/\tau}$ , where  $\sigma$  is the stress at any time instant  $t$ ,  $\sigma_0$  is the initial stress and  $\tau$  is the relaxation time. The relaxation process is temperature dependent and follows the Arrhenius law. For a rubber sample, the relaxation time is 60 days at 25°C.

Q.19 If the above sample is stressed to 2 MPa initially, then the time required to relax the stress to 1 MPa will be

(A) 31.6 days

(B) 41.6 days

(C) 51.6 days

(D) 61.6 days

Q.20 If the activation energy for relaxation is 30 KJ/mol, the relaxation time at 35°C will be

(A) 30.5 days

(B) 35.5 days

(C) 40.5 days

(D) 45.5 days

**Linked Answer Questions****Statement for Linked Answer Questions 21 and 22:**

In tensile testing of carbon fiber reinforced epoxy composite samples, the following data were recorded:

gauge length = 4 cm

cross-section = 0.8 cm × 0.3 cm

increase in gauge length at the break point = 0.03 cm

breaking load = 50 kg

Q.21 Considering the stress-strain curve to be linear up to the break point, the tensile strength is

(A) 191.2 kg/cm<sup>2</sup>

(B) 208.3 kg/cm<sup>2</sup>

(C) 312.1 kg/cm<sup>2</sup>

(D) 535.5 kg/cm<sup>2</sup>

Q.22 The Young's modulus of the composite is

(A)  $1.77 \times 10^4$  kg/cm<sup>2</sup>

(B)  $1.99 \times 10^4$  kg/cm<sup>2</sup>

(C)  $2.34 \times 10^4$  kg/cm<sup>2</sup>

(D)  $2.77 \times 10^4$  kg/cm<sup>2</sup>

**END OF SECTION - F**

**G : FOOD TECHNOLOGY****Q. 1 – Q. 9 carry one mark each.**

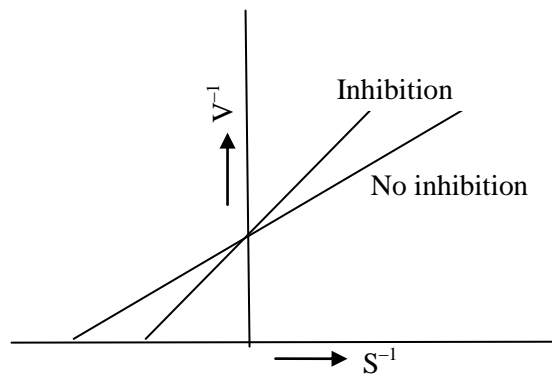
- Q.1 Among the following fatty acids, which group is known as essential fatty acids?
- (A) 9,11-Octadecadienoic and 9,11,13-Octadecatrienoic  
(B) 9,12-Octadecadienoic and 9,12,15-Octadecatrienoic  
(C) 9-Octadecenoic and 9,11-Octadecadienoic  
(D) 9,11-Octadecadienoic and 9-Eicosenoic
- Q.2 Cellulose, the structural polysaccharide of plant, is a polymer of
- (A)  $\beta$ -D-Glucose  
(B)  $\alpha$ -D-Glucose  
(C)  $\beta$ -D-Galactose  
(D)  $\alpha$ -D-Galcturonic acid
- Q.3 The important role of carotenoids in the human diet is their ability to serve as precursors of
- (A) Vitamin C                (B) Vitamin D                (C) Vitamin A                (D) Vitamin K
- Q.4 Which one of the following microorganisms is used in the preparation of bread?
- (A) *Candida utilis*    (B) *Saccharomyces cerevisiae*  
(C) *Saccharomyces cevarum*    (D) *Aspergillus niger*
- Q.5 Which one of the microorganisms given below is NOT RESPONSIBLE for ropy or stringy fermentation of milk?
- (A) *Alcaligenes viscolactis*  
(B) *Enterobacter aerogenes*  
(C) *Streptococcus cremoris*  
(D) *Streptococcus lactis*
- Q.6 A mild heat treatment of foods that destroys pathogens and extends its shelf life is called
- (A) Baking    (B) Blanching  
(C) Sterilization    (D) Pasteurization
- Q.7 The most common and least expensive plastic film used for packaging of solid food materials is
- (A) Polyethylene    (B) Polystyrene  
(C) Polypropylene    (D) Polyvinylchloride
- Q.8 Reassociation of amylose and formation of crystalline structure upon cooling of cooked starch solution is termed as
- (A) Syneresis    (B) Gelatinization  
(C) Retrogradation    (D) Denaturation
- Q.9 Thermal destruction of microorganisms follows a kinetics of
- (A) Zero order  
(B) First order  
(C) Second order  
(D) Fractional order

**Q. 10 - Q. 22 carry two marks each.**

Q.10 Which one of the following is NOT A CORRECT statement?

- (A) Meatiness is the taste produced by compounds such as glutamate in products like cheese, soy sauce.
- (B) Astringency is a dry mouth feel in the oral cavity that is most associated with phenolic compounds.
- (C) Saltiness is a taste that is mainly produced by chloride ions.
- (D) Sourness is related to acidity and is sensed by hydrogen ion channels in the human tongue.

Q.11 The following plot represents the *Lineweaver-Burk* equation of an enzymatic reaction both in the presence and the absence of inhibitor. Here,  $V$  is the velocity of reaction and  $S$  is the substrate concentration.



The nature of inhibition shown in the plot is

- (A) Non-competitive
- (B) Anti-competitive
- (C) Competitive
- (D) Mixed type

Q.12 Make the correct match of the food constituents in **Group I** with their nature given in **Group II**.

**Group I**

- P) Ascorbic Acid
- Q) Phenyl alanine
- R) Dextrose
- S) Haemoglobin

**Group II**

- 1) Sugar
- 2) Chelate
- 3) Amino Acid
- 4) Antioxidant

- (A) P-4, Q-3, R-1, S-2
- (B) P-4, Q-1, R-3, S-2
- (C) P-3, Q-4, R-2, S-1
- (D) P-4, Q-2, R-1, S-3

Q.13 Make the correct match of the fermented food products in **Group I** with the microorganisms in **Group II**.

**Group I**

- P) Yoghurt
- Q) Cheese
- R) Sauerkraut
- S) Kefir

**Group II**

- 1) *Lactobacillus acidophilus* and *Lactobacillus delbrueckii*
- 2) *Leuconostoc mesenteroides* and *Lactobacillus plantarum*
- 3) *Lactobacillus delbrueckii* and *Streptococcus thermophilus*
- 4) *Lactobacillus casei* and *Streptococcus thermophilus*

- (A) P-1, Q-4, R-2, S-3
- (B) P-4, Q-3, R-1, S-2
- (C) P-3, Q-4, R-2, S-1
- (D) P-3, Q-2, R-4, S-1

Q.14 Match the following between organelle or cellular components of a bacterium cell in **Group I** with the constituents and functionalities in **Group II**.

**Group I**

- P) Cytoplasmic membrane
- Q) Flagellum
- R) Cell wall
- S) Ribosome

**Group II**

- 1) Protein synthesis
- 2) Peptidoglycan
- 3) Phospholipid bilayer
- 4) Motility of cell

- (A) P-3, Q-2, R-4, S-1
- (B) P-4, Q-2, R-1, S-3
- (C) P-3, Q-4, R-2, S-1
- (D) P-2, Q-3, R-4, S-1

Q.15 Thermal death time (TDT) of *Clostridium botulinum* at 121 °C is 2.78 min with a z-value of 10 °C. The TDT of the microorganism at 116 °C (in min) is

- (A) 5.270
- (B) 8.791
- (C) 1.390
- (D) 0.712

Q.16 Make the correct match between specific food processing operations in **Group I** with their mechanism of action in **Group II**.

**Group I**

- P) Ball Mill
- Q) Roller Mill
- R) Flash Peeling
- S) Abrasive Peeling

**Group II**

- 1) Compression and shear
- 2) Pressure bursting
- 3) Friction and shear
- 4) Impact and shear

- (A) P-4, Q-2, R-1, S-3
- (B) P-4, Q-1, R-2, S-3
- (C) P-4, Q-3, R-2, S-1
- (D) P-3, Q-1, R-4, S-2

## Common Data Questions

### Common Data for Questions 17 and 18:

650 g of a wet food containing 405 g water is dried in a tray dryer to a final moisture content of 6.8 % (dry basis). It is observed that the drying process occurs under constant rate period and it takes 8 h.

Q.17 Initial moisture content (in percentage) of the food on wet basis is

- (A) 62.31
- (B) 70.45
- (C) 162.31
- (D) 165.31

Q.18 The rate of drying (in kg/h) is

- (A) 128.79
- (B) 126.35
- (C) 77.81
- (D) 0.0485

**Common Data for Questions 19 and 20:**

Air at 1 atmospheric pressure (101.325 kPa) and 30 °C with absolute humidity of 0.0218 kg/kg of dry air is flowing in a drying chamber. The saturated vapor pressure of water ( $p_w^0$ , in kPa) is related to temperature (T, in °C) as given below

$$\ln p_w^0 = 18.6556 - \frac{5217.635}{T + 273}$$

Heat capacities of dry air (average molecular weight 29) and that of water vapor (molecular weight 18) are 1.005 and 1.884 kJ/kg.K, respectively. Latent heat of vaporization of water at reference temperature (0 °C) is 2502.3 kJ/kg.

- Q.19 The relative humidity of air (in percentage) is  
(A) 62.82 (B) 68.22 (C) 86.62 (D) 81.80
- Q.20 The enthalpy (in kJ/kg) of moist air is  
(A) 85.93 (B) 54.55 (C) 31.38 (D) 99.38

**Linked Answer Questions****Statement for Linked Answer Questions 21 and 22:**

The total solids content in a milk sample is 18 %. It is desired to produce 1000 kg of sweetened condensed milk (SCM) having 40 % sugar, 25 % moisture and rest milk solids.

- Q.21 What is the 'Sugar Ratio' (in percentage) in the SCM in terms of sugar and water content in the final product?  
(A) 48.19 (B) 61.54 (C) 54.16 (D) 56.14
- Q.22 If the 'Concentration Degree' is 2.5, the amount of sugar added in kg in the milk sample is  
(A) 246.16 (B) 216.64 (C) 192.76 (D) 224.56

**END OF THE QUESTION PAPER**

## GATE 2012 - Answer Key - Paper : XE

Paper	Section	Question no.	Key
XE	GA	1	B
XE	GA	2	B
XE	GA	3	D
XE	GA	4	A
XE	GA	5	D
XE	GA	6	C
XE	GA	7	D
XE	GA	8	A
XE	GA	9	A
XE	GA	10	A
XE	A	1	A
XE	A	2	C
XE	A	3	B
XE	A	4	D
XE	A	5	C
XE	A	6	D
XE	A	7	C
XE	A	8	D
XE	A	9	C
XE	A	10	B
XE	A	11	B
XE	B	1	D
XE	B	2	A
XE	B	3	D
XE	B	4	D
XE	B	5	D
XE	B	6	C
XE	B	7	D
XE	B	8	B
XE	B	9	C
XE	B	10	A
XE	B	11	A
XE	B	12	C
XE	B	13	D
XE	B	14	A
XE	B	15	C
XE	B	16	B
XE	B	17	B
XE	B	18	C
XE	B	19	B
XE	B	20	C
XE	B	21	A
XE	B	22	B

Paper	Section	Question no.	Key
XE	C	1	D
XE	C	2	C
XE	C	3	A
XE	C	4	B
XE	C	5	A
XE	C	6	C
XE	C	7	B
XE	C	8	D
XE	C	9	A
XE	C	10	B
XE	C	11	A
XE	C	12	D
XE	C	13	C
XE	C	14	D
XE	C	15	B
XE	C	16	C
XE	C	17	A
XE	C	18	B
XE	C	19	D
XE	C	20	Marks to All
XE	C	21	B
XE	C	22	C
XE	D	1	A
XE	D	2	A
XE	D	3	D
XE	D	4	C
XE	D	5	B
XE	D	6	B
XE	D	7	B
XE	D	8	C
XE	D	9	C
XE	D	10	C
XE	D	11	D
XE	D	12	C
XE	D	13	Marks to All
XE	D	14	C
XE	D	15	Marks to All
XE	D	16	D
XE	D	17	Marks to All
XE	D	18	A
XE	D	19	B
XE	D	20	Marks to All
XE	D	21	B
XE	D	22	A



## GATE 2012 - Answer Key - Paper : XE

Paper	Section	Question no.	Key
XE	E	1	B
XE	E	2	D
XE	E	3	A
XE	E	4	D
XE	E	5	B
XE	E	6	C
XE	E	7	A
XE	E	8	C
XE	E	9	A
XE	E	10	B
XE	E	11	B
XE	E	12	D
XE	E	13	A
XE	E	14	B
XE	E	15	C
XE	E	16	C
XE	E	17	D
XE	E	18	C
XE	E	19	B
XE	E	20	C
XE	E	21	A
XE	E	22	D
XE	F	1	B
XE	F	2	C
XE	F	3	A
XE	F	4	D
XE	F	5	A
XE	F	6	C
XE	F	7	B
XE	F	8	C
XE	F	9	D
XE	F	10	C
XE	F	11	A
XE	F	12	A
XE	F	13	B
XE	F	14	D
XE	F	15	B
XE	F	16	C
XE	F	17	C
XE	F	18	A
XE	F	19	B
XE	F	20	C
XE	F	21	B
XE	F	22	D

Paper	Section	Question no.	Key
XE	G	1	B
XE	G	2	A
XE	G	3	C
XE	G	4	B
XE	G	5	D
XE	G	6	D
XE	G	7	A
XE	G	8	C
XE	G	9	B
XE	G	10	C
XE	G	11	C
XE	G	12	A
XE	G	13	C
XE	G	14	C
XE	G	15	B
XE	G	16	B
XE	G	17	A
XE	G	18	D
XE	G	19	D
XE	G	20	A
XE	G	21	B
XE	G	22	A